

# SpringBoard

# Unit Activity Correlations to Common Core State Standards

# Algebra 2

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# Number and Quantity

### The Complex Number System

#### Perform arithmetic operations with complex numbers.

**1.** Know there is a complex number i such that  $i^2 = -1$ , and every complex number has the form a + bi with a and b real.

Unit 3, Unit OverviewUnit 3, Unit Overview Unit 3, Activity 3-3: Introduction to Complex Numbers Unit 3, Activity 3-4: Solving ax2 + bx + c = 0 Unit 3, Activity 3-5: Graphing Quadratics and Quadratic Inequalities Unit 3, Unit Practice Unit 3, Unit Reflection Unit 4, Getting Ready Unit 4, Activity 4-3: Factors of Polynomials Unit 4, Unit Practice

# 2. Use the relation $i^2 = -1$ and the commutative, associative, and distributive properties to add, subtract, and multiply complex numbers.

Unit 3, Unit Overview Unit 3, Activity 3-3: Introduction to Complex Numbers Unit 3, Activity 3-4: Solving ax2 + bx + c = 0 Unit 3, Unit Practice Unit 3, Unit Reflection Unit 4, Getting Ready Unit 4, Activity 4-3: Factors of Polynomials Unit 4, Unit Practice

#### Use complex numbers in polynomial identities and equations.

7. Solve quadratic equations with real coefficients that have complex solutions.

Unit 3, Unit Overview Unit 3, Activity 3-1: Applications of Quadratic Functions Unit 3, Activity 3-4: Solving ax2 + bx + c = 0 Unit 3, EA 3-1: Applications of Quadratic Function Unit 3, Unit Practice Unit 3, Math Standards Review

#### 8. Extend polynomial identities to the complex numbers. For example, rewrite $x^2 + 4$ as (x + 2i)(x - 2i).

Unit 3, Activity 3-3: Introduction to Complex Numbers Unit 3, Unit Practice Unit 5, Activity 5-3: Rational Exponents and Radical Expressions

#### 9. Know the Fundamental Theorem of Algebra; show that it is true for quadratic polynomials.

Unit 4, Activity 4-3: Factors of Polynomials Unit 4, Activity 4-4: Graphs of Polynomials Unit 5, Activity 5-7: Rational Equations and Inequalities

# <u>Algebra</u>

## Seeing Structure in Expressions

#### Interpret the structure of expressions

1. Interpret expressions that represent a quantity in terms of its context.

a. Interpret parts of an expression, such as terms, factors, and coefficients.

Unit 1, Activity 1-4: Function Composition and Operations Unit 1, Activity 1-5 Inverse Functions Unit 2, Getting Ready Unit 2, Activity 2-5: Inverse Functions Unit 2, Activity 2-6: Logarithmic and Exponential Equations and Inequalities Unit 2, Math Standards Review Unit 3, Activity 3-2: Factoring and Solving Quadratics Unit 3, Activity 3-3: Introduction to Complex Numbers Unit 3, Activity 3-4: Solving ax2 + bx + c = 0 Unit 4, Getting Ready Unit 4, Activity 4-1: Introduction to Polynomials Unit 4, Activity 4-3: Factors of Polynomials

Unit 4, Activity 4-4: Graphs of Polynomials Unit 4, Activity 4-6: Combinations and Permutations Unit 5, Getting Ready Unit 5, Activity 5-3: Rational Exponents and Radical Expressions Unit 5, Activity 5-6: Simplifying Rational Expressions Unit 5, EA 5-2: Rational Equations and Functions Unit 5, Unit Practice Unit 5, Unit Reflection Unit 5, Math Standards Review Unit 7, Getting Ready Unit 7, Activity 7-2: Ellipses and Circles

# b. Interpret complicated expressions by viewing one or more of their parts as a single entity. For example, interpret P(1+r)n as the product of P and a factor not depending on P.

Unit 1, Activity 1-4: Function Composition and Operations Unit 1, Activity 1-5 Inverse Functions Unit 2, Getting Ready Unit 2, Activity 2-5: Inverse Functions Unit 2, Activity 2-6: Logarithmic and Exponential Equations and Inequalities Unit 2, Math Standards Review Unit 3, Activity 3-3: Introduction to Complex Numbers Unit 3, Activity 3-4: Solving ax2 + bx + c = 0 Unit 4, Getting Ready Unit 4, Activity 4-3: Factors of Polynomials Unit 4, Activity 4-4: Graphs of Polynomials

Unit 4, Activity 4-6: Combinations and Permutations Unit 5, Getting Ready Unit 5, Activity 5-3: Rational Exponents and Radical Expressions Unit 5, Activity 5-6: Simplifying Rational Expressions Unit 5, EA 5-2: Rational Equations and Functions Unit 5, Unit Practice Unit 5, Unit Reflection Unit 5, Math Standards Review Unit 7, Getting Ready Unit 7, Activity 7-2: Ellipses and Circles

# 2. Use the structure of an expression to identify ways to rewrite it. For example, see $x^4 - y^4$ as $(x^2)^2 - (y^2)^2$ , thus recognizing it as a difference of squares that can be factored as $(x^2 - y^2)(x^2 + y^2)$ .

Unit 1, Activity 1-4: Function Composition and Operations Unit 1, Activity 1-5 Inverse Functions Unit 2, Getting Ready Unit 2, Activity 2-5: Inverse Functions Unit 2, Activity 2-6: Logarithmic and Exponential Equations and Inequalities Unit 2, Math Standards Review Unit 3, Activity 3-3: Introduction to Complex Numbers Unit 3, Activity 3-4: Solving ax2 + bx + c = 0 Unit 4, Getting Ready Unit 4, Activity 4-4: Graphs of Polynomials Unit 5, Getting Ready Unit 5, Activity 5-3: Rational Exponents and Radical Expressions Unit 5, Activity 5-6: Simplifying Rational Expressions Unit 5, EA 5-2: Rational Equations and Functions Unit 5, Unit Practice Unit 5, Unit Reflection Unit 5, Math Standards Review Unit 7, Getting Ready Unit 7, Activity 7-2: Ellipses and Circles

#### Write expressions in equivalent forms to solve problems

4. Derive the formula for the sum of a finite geometric series (when the common ratio is not 1), and use the formula to solve problems. For example, calculate mortgage payments.

Unit 2, Activity 2-2: Geometric Sequences and Series Unit 2, EA 2-1: Sequences and Series Unit 2, Unit Practice Unit 2, Unit Reflection Unit 2, Math Standards Review

### Arithmetic with Polynomials and Rational Expressions

#### Perform arithmetic operations on polynomials

**1.** Understand that polynomials form a system analogous to the integers, namely, they are closed under the operations of addition, subtraction, and multiplication; add, subtract, and multiply polynomials.

Unit 3, Getting Ready Unit 3, Activity 3-1: Applications of Quadratic Functions Unit 3, Activity 3-2: Factoring and Solving Quadratics Unit 4, Unit Overview Unit 4, Activity 4-2: Polynomial Operations Unit 4, EA 4-1: Polynomial Operations Unit 4, Activity 4-3: Factors of Polynomials Unit 5, Getting Ready Unit 5, Activity 5-1: Composition of Functions Unit 5, Activity 5-2: Graphing Square Root Functions Unit 5, Activity 5-6: Simplifying Rational Expressions Unit 5, Unit Practice Unit 5, Unit Reflection

#### Understand the relationship between zeros and factors of polynomials

2. Know and apply the Remainder Theorem: For a polynomial p(x) and a number a, the remainder on division by x - a is p(a), so p(a) = 0 if and only if (x - a) is a factor of p(x).

Unit 3, Activity 3-1: Applications of Quadratic Functions Unit 3, Activity 3-2: Factoring and Solving Quadratics Unit 3, Activity 3-3: Introduction to Complex Numbers Unit 3, EA 3-2: Graphs of Quadratic Functions Unit 3, Unit Practice Unit 4, Activity 4-3: Factors of Polynomials Unit 4, Activity 4-4: Graphs of Polynomials Unit 4, Unit Practice Unit 4, Unit Reflection Unit 4, Math Standards Review

**3.** Identify zeros of polynomials when suitable factorizations are available, and use the zeros to construct a rough graph of the function defined by the polynomial.

Unit 4, Activity 4-3: Factors of Polynomials Unit 4, Activity 4-4: Graphs of Polynomials Unit 4, EA 4-2: Factoring and Graphing Polynomials Unit 4, Unit Practice

#### Use polynomial identities to solve problems

4. Prove polynomial identities and use them to describe numerical relationships. For example, the polynomial identity  $(x^2 + y^2)^2 = (x^2 - y^2)^2 + (2xy)^2$  can be used to generate Pythagorean triples.

Precalculus, Unit 1, Activity 1-1: Arithmetic Sequences

5. Know and apply the Binomial Theorem for the expansion of (x + y)n in powers of x and y for a positive integer n, where x and y are any numbers, with coefficients determined for example by Pascal's Triangle.

Unit 4, Activity 4-6: Combinations and Permutations Unit 4, EA 4-3: Combinations, Permutations and Probability Unit 4, Unit Practice Unit 4, Unit Reflection

#### **Rewrite rational expressions**

6. Rewrite simple rational expressions in different forms; write a(x)/b(x) in the form q(x) + r(x)/b(x), where a(x), b(x), q(x), and r(x) are polynomials with the degree of r(x) less than the degree of b(x), using inspection, long division, or, for the more complicated examples, a computer algebra system.

Unit 4, Activity 4-1: Introduction to Polynomials Unit 4, Activity 4-2: Polynomial Operations Unit 4, EA 4-1: Polynomial Operations Unit 5, Activity 5-1: Composition of Functions Unit 5, Activity 5-4: Introduction to Rational Functions Unit 5, Activity 5-5: Inverse Variation and Rational Functions Unit 5, Activity 5-6: Simplifying Rational Expressions Unit 5, Activity 5-7: Rational Equations and Inequalities Unit 5, EA 5-2: Rational Equations and Functions

#### Unit 5, Unit Practice Unit 5, Unit Reflection Unit 5, Math Standards Review Unit 7, Activity 7-1: The Conic Sections Unit 7, Activity 7-2: Ellipses and Circles Unit 7, Activity 7-3: Hyperbolas Unit 7, Activity 7-5: Identifying Conic Sections Unit 7, EA 7-1: Conic Sections Unit 7, Unit Practice

# 7. Understand that rational expressions form a system analogous to the rational numbers, closed under addition, subtraction, multiplication, and division by a nonzero rational expression; add, subtract, multiply, and divide rational expressions.

- Unit 4, Activity 4-1: Introduction to Polynomials Unit 4, Activity 4-2: Polynomial Operations Unit 4, EA 4-1: Polynomial Operations Unit 5, Activity 5-1: Composition of Functions Unit 5, Activity 5-4: Introduction to Rational Functions Unit 5, Activity 5-5: Inverse Variation and Rational Functions Unit 5, Activity 5-6: Simplifying Rational Expressions Unit 5, Activity 5-7: Rational Equations and Inequalities Unit 5, EA 5-2: Rational Equations and Functions
- Unit 5, Unit Practice Unit 5, Unit Reflection Unit 5, Math Standards Review Unit 7, Activity 7-1: The Conic Sections Unit 7, Activity 7-2: Ellipses and Circles Unit 7, Activity 7-3: Hyperbolas Unit 7, Activity 7-5: Identifying Conic Sections Unit 7, EA 7-1: Conic Sections Unit 7, Unit Practice

### **Creating Equations**

#### Create equations that describe numbers or relationships

**1.** Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.

Unit 1, Activity 1-3: Absolute Value and Piecewise-Defined Functions Unit 2, Activity 2-6: Logarithmic and Exponential Equations and Inequalities Unit 3, Activity 3-3: Introduction to Complex Numbers Unit 5, Activity 5-2: Graphing Square Root Functions Unit 5, Activity 5-3: Rational Exponents and Radical Expressions Unit 5, Activity 5-7: Rational Equations and Inequalities Unit 6, Activity 6-3: Normal Distribution Unit 6, EA 6-2: Data Modeling and Normal Distribution Unit 6, Unit Practice Unit 7, Unit Practice

# 2. Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.

Unit 1, Getting Ready Unit 1, Activity 1-1: Linear Programming Choices Unit 1, Activity 1-2: Systems of Linear Equations Unit 1, EA 1-1: Linear Programming and Systems Unit 1, Activity 1-4: Function Composition and Operations Unit 2, Activity 2-3: Exponential Function and Graphs Unit 2, Activity 2-4: Common Logarithms and Their Properties Unit 2, Activity 2-6: Logarithmic and Exponential Equations and Inequalities

Unit 5, Activity 5-4: Introduction to Rational Functions Unit 5, Activity 5-5: Inverse Variation and Rational Functions **3.** Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context. For example, represent inequalities describing nutritional and cost constraints on combinations of different foods.

Unit 1, Activity 1-1: Linear Programming Choices Unit 1, EA 1-1: Linear Programming and Systems Unit 1, Unit Practice Unit 5, Activity 5-4: Introduction to Rational Functions Unit 5, Activity 5-5: Inverse Variation and Rational Functions Unit 5, Activity 5-6: Simplifying Rational Expressions Unit 5, Activity 5-7: Rational Equations and Inequalities Unit 5, EA 5-2: Rational Equations and Functions Unit 5, Unit Practice Unit 5, Unit Reflection Unit 7, Activity 7-3: Hyperbolas Unit 7, Activity 7-5: Identifying Conic Sections Unit 7, Unit Practice

4. Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations. For example, rearrange Ohm's law V = IR to highlight resistance R.

Unit 5, Activity 5-1: Composition of Functions

### **Reasoning with Equations and Inequalities**

Understand solving equations as a process of reasoning and explain the reasoning

**2.** Solve simple rational and radical equations in one variable, and give examples showing how extraneous solutions may arise.

Unit 5, Activity 5-2: Graphing Square Root Functions Unit 5, Activity 5-3: Rational Exponents and Radical Expressions Unit 5, EA 5-1: Square Root Expressions, Equations, and Functions Unit 5, Activity 5-4: Introduction to Rational Functions Unit 5, Activity 5-5: Inverse Variation and Rational Functions Unit 5, Activity 5-6: Simplifying Rational Expressions Unit 5, Activity 5-7: Rational Equations and Inequalities Unit 5, EA 5-2: Rational Equations and Functions Unit 5, Unit Practice Unit 5, Unit Reflection

#### Represent and solve equations and inequalities graphically

11. Explain why the x-coordinates of the points where the graphs of the equations y = f(x) and y = g(x) intersect are the solutions of the equation f(x) = g(x); find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where f(x) and/or g(x) are linear, polynomial, rational, absolute value, exponential, and logarithmic functions.

Unit 1, Activity 1-1: Linear Programming Choices

# **Functions**

### **Interpreting Functions**

#### Interpret functions that arise in applications in terms of the context

4. For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.

Unit 1, Getting Ready Unit 1, Activity 1-1: Linear Programming Choices Unit 1, Activity 1-2: Systems of Linear Equations Unit 1, EA 1-1: Linear Programming and Systems Unit 1, Activity 1-3: Absolute Value and Piecewise-Defined **Functions** Unit 1, Activity 1-4: Function Composition and Operations Unit 1, Activity 1-5 Inverse Functions Unit 1, EA 1-2: Composite and Inverse Functions Unit 1, Unit Practice Unit 1, Unit Reflection Unit 1, Math Standards Review Unit 2, Getting Ready Unit 2, Activity 2-1: Arithmetic Sequences and Series Unit 2, Activity 2-2: Geometric Sequences and Series Unit 2, EA 2-1: Sequences and Series Unit 2, Activity 2-3: Exponential Function and Graphs Unit 2, Activity 2-4: Common Logarithms and Their Properties Unit 2, EA 2-2: Exponential Functions and Common Logarithms Unit 2, Activity 2-5: Inverse Functions Unit 2, Activity 2-6: Logarithmic and Exponential Equations and Inequalities Unit 2, EA 2-3: Exponential and Logarithmic Equations Unit 2, Unit Practice Unit 2, Unit Reflection Unit 2, Math Standards Review Unit 3, Getting Ready Unit 3, Activity 3-1: Applications of Quadratic Functions Unit 3, Activity 3-2: Factoring and Solving Quadratics Unit 3, Activity 3-3: Introduction to Complex Numbers Unit 3, Activity 3-4: Solving  $ax^2 + bx + c = 0$ 

Unit 3, EA 3-1: Applications of Quadratic Function Unit 3, Activity 3-5: Graphing Quadratics and Quadratic Inequalities Unit 3, Activity 3-6: Transformations of y = x2 Unit 3, EA 3-2: Graphs of Quadratic Functions Unit 3, Unit Practice Unit 3, Unit Reflection Unit 3, Math Standards Review Unit 4, Getting Ready Unit 4, Activity 4-1: Introduction to Polynomials Unit 4, Activity 4-2: Polynomial Operations Unit 4, EA 4-1: Polynomial Operations Unit 4, Activity 4-3: Factors of Polynomials Unit 4, Activity 4-4: Graphs of Polynomials Unit 4, EA 4-2: Factoring and Graphing Polynomials Unit 5, Getting Ready Unit 5, Activity 5-1: Composition of Functions Unit 5, Activity 5-2: Graphing Square Root Functions Unit 5, Activity 5-3: Rational Exponents and Radical Expressions Unit 5, EA 5-1: Square Root Expressions, Equations, and **Functions** Unit 5, Activity 5-4: Introduction to Rational Functions Unit 5, Activity 5-5: Inverse Variation and Rational Functions Unit 5, Activity 5-6: Simplifying Rational Expressions Unit 5, Activity 5-7: Rational Equations and Inequalities Unit 5, EA 5-2: Rational Equations and Functions Unit 5, Unit Practice Unit 5, Unit Reflection Unit 5, Math Standards Review Unit 7, Activity 7-4: Parabolas

5. Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes. For example, if the function h(n) gives the number of person-hours it takes to assemble n engines in a factory, then the positive integers would be an appropriate domain for the function.

Unit 1, Activity 1-1: Linear Programming Choices Unit 1, Activity 1-3: Absolute Value and Piecewise-Defined Functions

Unit 1, Activity 1-4: Function Composition and Operations Unit 1, Activity 1-5 Inverse Functions Unit 1, Unit Practice Unit 2, Activity 2-1: Arithmetic Sequences and Series Unit 2, Activity 2-2: Geometric Sequences and Series Unit 2, EA 2-1: Sequences and Series Unit 2, Activity 2-3: Exponential Function and Graphs

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Unit 2, EA 2-2: Exponential Functions and Common Unit 3, EA 3-2: Graphs of Quadratic Functions Logarithms Unit 3, Unit Practice Unit 2, Activity 2-5: Inverse Functions Unit 4, Activity 4-4: Graphs of Polynomials Unit 2, Activity 2-6: Logarithmic and Exponential Equations Unit 4, EA 4-2: Factoring and Graphing Polynomials Unit 5, Activity 5-2: Graphing Square Root Functions and Inequalities Unit 2, EA 2-3: Exponential and Logarithmic Equations Unit 5, EA 5-1: Square Root Expressions, Equations, and Unit 2, Unit Practice Functions Unit 3, Activity 3-5: Graphing Quadratics and Quadratic Unit 5, Activity 5-4: Introduction to Rational Functions Unit 5, Activity 5-5: Inverse Variation and Rational Functions Inequalities Unit 3, Activity 3-6: Transformations of  $y = x^2$ Unit 5, EA 5-2: Rational Equations and Functions

# 6. Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.

Unit 1, Activity 1-1: Linear Programming Choices Unit 1, Activity 1-4: Function Composition and Operations Unit 2, Unit Overview Unit 2, Activity 2-2: Geometric Sequences and Series Unit 2, EA 2-1: Sequences and Series Unit 2, Activity 2-3: Exponential Function and Graphs Unit 5, Activity 5-4: Introduction to Rational Functions Unit 6, Activity 6-4: Data Modeling Unit 6, EA 6-2: Data Modeling and Normal Distribution Unit 6, Unit Practice

#### Analyze functions using different representations

7. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.

b. Graph square root, cube root, and piecewise-defined functions, including step functions and absolute value functions.

Unit 1, Activity 1-3: Absolute Value and Piecewise-Defined Functions Unit 1, Activity 1-4: Function Composition and Operations Unit 1, Unit Practice Unit 5, Activity 5-2: Graphing Square Root Functions Unit 5, EA 5-1: Square Root Expressions, Equations, and Functions Unit 5, Unit Practice

#### c. Graph polynomial functions, identifying zeros when suitable factorizations are available, and showing end behavior.

Unit 4, Activity 4-4: Graphs of Polynomials Unit 4, EA 4-2: Factoring and Graphing Polynomials

e. Graph exponential and logarithmic functions, showing intercepts and end behavior, and trigonometric functions, showing period, midline, and amplitude.

Unit 2, Activity 2-3: Exponential Function and Graphs Unit 2, EA 2-2: Exponential Functions and Common Logarithms Unit 2, Activity 2-5: Inverse Functions Unit 2, Activity 2-6: Logarithmic and Exponential Equations and Inequalities Unit 2, EA 2-3: Exponential and Logarithmic Equations Unit 2, Unit Practice

# 8. Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function.

a. Use the process of factoring and completing the square in a quadratic function to show zeros, extreme values, and symmetry of the graph, and interpret these in terms of a context.

Unit 3, Getting Ready Unit 3, Activity 3-1: Applications of Quadratic Functions Unit 3, Activity 3-2: Factoring and Solving Quadratics Unit 3, Activity 3-3: Introduction to Complex Numbers Unit 3, Activity 3-4: Solving ax2 + bx + c = 0 Unit 3, EA 3-1: Applications of Quadratic Function Unit 3, Activity 3-5: Graphing Quadratics and Quadratic Inequalities

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Unit 3, Activity 3-6: Transformations of y = x2 Unit 3, EA 3-2: Graphs of Quadratic Functions Unit 3, Unit Practice Unit 3, Unit Reflection Unit 5, Getting Ready Unit 5, Activity 5-6: Simplifying Rational Expressions Unit 7, Getting Ready

b. Use the properties of exponents to interpret expressions for exponential functions. For example, identify percent rate of change in functions such as y = (1.02)t, y = (0.97)t, y = (1.01)12t, y = (1.2)t/10, and classify them as representing exponential growth or decay.

Unit 2, Unit Overview Unit 2, Activity 2-3: Exponential Function and Graphs Unit 2, Activity 2-4: Common Logarithms and Their Properties Unit 2, EA 2-2: Exponential Functions and Common Logarithms Unit 2, Unit Reflection

9. Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions). For example, given a graph of one quadratic function and an algebraic expression for another, say which has the larger maximum.

Unit 1, Getting Ready Unit 1, Activity 1-1: Linear Programming Choices Unit 1, Activity 1-2: Systems of Linear Equations Unit 1, EA 1-1: Linear Programming and Systems Unit 1, Activity 1-3: Absolute Value and Piecewise-Defined Functions Unit 1, Activity 1-4: Function Composition and Operations Unit 1, Activity 1-5 Inverse Functions Unit 1, EA 1-2: Composite and Inverse Functions Unit 1. Unit Practice Unit 1, Unit Reflection Unit 1, Math Standards Review Unit 2, Activity 2-3: Exponential Function and Graphs Unit 2, EA 2-2: Exponential Functions and Common Logarithms Unit 2, Activity 2-5: Inverse Functions Unit 2, Activity 2-6: Logarithmic and Exponential Equations and Inequalities Unit 2, EA 2-3: Exponential and Logarithmic Equations Unit 2, Unit Practice Unit 3, Getting Ready Unit 3, Activity 3-1: Applications of Quadratic Functions Unit 3, EA 3-1: Applications of Quadratic Function

Unit 3, Activity 3-5: Graphing Quadratics and Quadratic Inequalities Unit 3, Activity 3-6: Transformations of y = x2 Unit 3, EA 3-2: Graphs of Quadratic Functions Unit 3, Unit Practice Unit 3, Unit Reflection Unit 3, Math Standards Review Unit 4, Activity 4-4: Graphs of Polynomials Unit 4, EA 4-2: Factoring and Graphing Polynomials Unit 4, Unit Practice Unit 5, Activity 5-1: Composition of Functions Unit 5, Activity 5-2: Graphing Square Root Functions Unit 5, Activity 5-3: Rational Exponents and Radical Expressions Unit 5, EA 5-1: Square Root Expressions, Equations, and **Functions** Unit 5, Activity 5-4: Introduction to Rational Functions Unit 5, Activity 5-5: Inverse Variation and Rational Functions Unit 5, EA 5-2: Rational Equations and Functions Unit 5, Unit Practice Unit 5, Unit Reflection Unit 5, Math Standards Review

### **Building Functions**

#### Build a function that models a relationship between two quantities

1. Write a function that describes a relationship between two quantities.

b. Combine standard function types using arithmetic operations. For example, build a function that models the temperature of a cooling body by adding a constant function to a decaying exponential, and relate these functions to the model.

Unit 1, Unit Overview Unit 1, Activity 1-2: Systems of Linear Equations Unit 1, EA 1-1: Linear Programming and Systems Unit 1, Activity 1-4: Function Composition and Operations

Unit 1, Activity 1-5 Inverse Functions Unit 1, EA 1-2: Composite and Inverse Functions Unit 1, Activity 1-7: Matrix Properties and Equations Unit 1, Unit Practice

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Unit 1, Unit Reflection Unit 2, Activity 2-5: Inverse Functions Unit 5, Unit Overview Unit 5, Getting Ready Unit 5, Activity 5-1: Composition of Functions

#### Build new functions from existing functions

Unit 5, EA 5-1: Square Root Expressions, Equations, and Functions Unit 5, Unit Practice Unit 5, Math Standards Review

3. Identify the effect on the graph of replacing f(x) by f(x) + k, k f(x), f(kx), and f(x + k) for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them.

Unit 1, Activity 1-3: Absolute Value and Piecewise-Defined Functions Unit 2, Activity 2-3: Exponential Function and Graphs Unit 2, Activity 2-5: Inverse Functions Unit 2, EA 2-3: Exponential and Logarithmic Equations Unit 2, Unit Practice Unit 3, Activity 3-6: Transformations of y = x2 Unit 5, Activity 5-2: Graphing Square Root Functions Unit 5, Activity 5-5: Inverse Variation and Rational Functions

#### 4. Find inverse functions.

a. Solve an equation of the form f(x) = c for a simple function f that has an inverse and write an expression for the inverse. For example,  $f(x) = 2x^3$  or f(x) = (x+1)/(x-1) for  $x \neq 1$ .

Unit 1, Activity 1-5 Inverse Functions Unit 1, Unit Practice Unit 2, Activity 2-4: Common Logarithms and Their Properties Unit 2, Activity 2-5: Inverse Functions Unit 5, Activity 5-1: Composition of Functions

Unit 5, EA 5-1: Square Root Expressions, Equations, and Functions Unit 5, EA 5-2: Rational Equations and Functions Unit 5, Unit Practice

### Linear, Quadratic, and Exponential Models

#### Construct and compare linear, quadratic, and exponential models and solve problems

4. For exponential models, express as a logarithm the solution to abct = d where a, c, and d are numbers and the base b is 2, 10, or e; evaluate the logarithm using technology.

Unit 2, Unit Overview Unit 2, Activity 2-3: Exponential Function and Graphs Unit 2, Activity 2-4: Common Logarithms and Their Properties Unit 2, EA 2-2: Exponential Functions and Common Logarithms Unit 2, Activity 2-5: Inverse Functions Unit 2, Activity 2-6: Logarithmic and Exponential Equations and Inequalities Unit 2, EA 2-3: Exponential and Logarithmic Equations Unit 2, Unit Practice

### **Trigonometric Functions**

Extend the domain of trigonometric functions using the unit circle

1. Understand radian measure of an angle as the length of the arc on the unit circle subtended by the angle.

Unit 3, Activity 3-1: Angles and Angle Measure

**2.** Explain how the unit circle in the coordinate plane enables the extension of trigonometric functions to all real numbers, interpreted as radian measures of angles traversed counterclockwise around the unit circle.

Unit 3, Activity 3-1: Angles and Angle Measure Unit 3, Activity 3-2: Sinusoidal Functions Unit 3, Activity 3-3: Trigonometric Functions and the Unit Circle

#### Model periodic phenomena with trigonometric functions

5. Choose trigonometric functions to model periodic phenomena with specified amplitude, frequency, and midline.

Unit 3, Activity 3-2: Sinusoidal Functions Unit 3, Activity 3-3: Trigonometric Functions and the Unit Circle Unit 3, Activity 3-7: Solving Simple Trigonometric Equations

#### Prove and apply trigonometric identities

8. Prove the Pythagorean identity  $sin2(\theta) + cos2(\theta) = 1$  and use it to find  $sin(\theta)$ ,  $cos(\theta)$ , or  $tan(\theta)$  given  $sin(\theta)$ ,  $cos(\theta)$ , or  $tan(\theta)$  and the quadrant of the angle.

Precalculus, Unit 4, Activity 4-1: Trigonometric Identities Precalculus, Unit 4, Activity 4-2: Identities and Equations

### **Statistics and Probability**

### **Interpreting Categorical and Quantitative Data**

Summarize, represent, and interpret data on a single count or measurement variable 4. Use the mean and standard deviation of a data set to fit it to a normal distribution and to estimate population percentages. Recognize that there are data sets for which such a procedure is not appropriate. Use calculators, spreadsheets, and tables to estimate areas under the normal curve.

Unit 6, Activity 6-2: Experiments and Randomization Unit 6, EA 6-1: Surveys and Results Unit 6, Activity 6-3: Normal Distribution Unit 6, Unit Practice Unit 6, Unit Reflection Unit 6, Math Standards Review

### **Making Inferences and Justifying Conclusions**

**Understand and evaluate random processes underlying statistical experiments** 1. Understand statistics as a process for making inferences about population parameters based on a random sample from that population.

Unit 6, Activity 6-1: Observational Study Unit 6, Activity 6-2: Experiments and Randomization Unit 6, EA 6-1: Surveys and Results Unit 6, Activity 6-3: Normal Distribution Unit 6, Unit Reflection

2. Decide if a specified model is consistent with results from a given data-generating process, e.g., using simulation. For example, a model says a spinning coin falls heads up with probability 0.5. Would a result of 5 tails in a row cause you to question

Unit 4, Activity 4-6: Combinations and Permutations Unit 6, Getting Ready Unit 6, Activity 6-1: Observational Study Unit 6, Activity 6-2: Experiments and Randomization Unit 6, EA 6-2: Data Modeling and Normal Distribution Unit 6, Activity 6-3: Normal Distribution

# Make inferences and justify conclusions from sample surveys, experiments, and observational studies

**3.** Recognize the purposes of and differences among sample surveys, experiments, and observational studies; explain how randomization relates to each.

Unit 4, Activity 4-5: Counting Methods Unit 4, Activity 4-7: Binomial Probability Unit 4, EA 4-3: Combinations, Permutations and Probability Unit 4, Unit Practice Unit 6, Unit Overview Unit 6, Getting Ready

Unit 6, Activity 6-1: Observational Study Unit 6, Activity 6-2: Experiments and Randomization Unit 6, EA 6-1: Surveys and Results Unit 6, Unit Practice Unit 6, Unit Reflection

# 4. Use data from a sample survey to estimate a population mean or proportion; develop a margin of error through the use of simulation models for random sampling.

Unit 6, Unit Overview Unit 6, Activity 6-1: Observational Study Unit 6, EA 6-1: Surveys and Results Algebra 1, Unit 6, Activity 6-1: Measures of Center and Spread Algebra 1, Unit 6, Activity 6-4: Developing a Survey Geometry, Unit 4, Activity 4-2: Arcs, Central and Inscribed Angles

# **5.** Use data from a randomized experiment to compare two treatments; use simulations to decide if differences between parameters are significant.

Unit 3, Unit Overview Unit 4, Activity 4-5: Counting Methods Unit 4, Activity 4-7: Binomial Probability Unit 4, EA 4-3: Combinations, Permutations and Probability Unit 4, Unit Practice Unit 6, Unit Overview Unit 6, Getting Ready

Unit 6, Activity 6-1: Observational Study Unit 6, Activity 6-2: Experiments and Randomization Unit 6, EA 6-1: Surveys and Results Unit 6, Activity 6-3: Normal Distribution Unit 6, Unit Practice Unit 6, Unit Reflection

#### 6. Evaluate reports based on data.

Unit 6, Activity 6-1: Observational Study Unit 6, Activity 6-2: Experiments and Randomization Unit 6, EA 6-1: Surveys and Results Unit 6, Activity 6-3: Normal Distribution

Unit 6, Activity 6-4: Data Modeling Unit 6, EA 6-2: Data Modeling and Normal Distribution Unit 6, Unit Practice

### **Using Probability to Make Decisions**

#### Use probability to evaluate outcomes of decisions

6. Use probabilities to make fair decisions (e.g., drawing by lots, using a random number generator).

Unit 4, Activity 4-7: Binomial Probability Unit 6, Activity 6-2: Experiments and Randomization Unit 6, Activity 6-3: Normal Distribution Unit 6, Unit Practice

# 7. Analyze decisions and strategies using probability concepts (e.g., product testing, medical testing, pulling a hockey goalie at the end of a game).

Unit 4, Activity 4-7: Binomial Probability Unit 6, Activity 6-2: Experiments and Randomization Unit 6, Activity 6-3: Normal Distribution Unit 6, Unit Practice